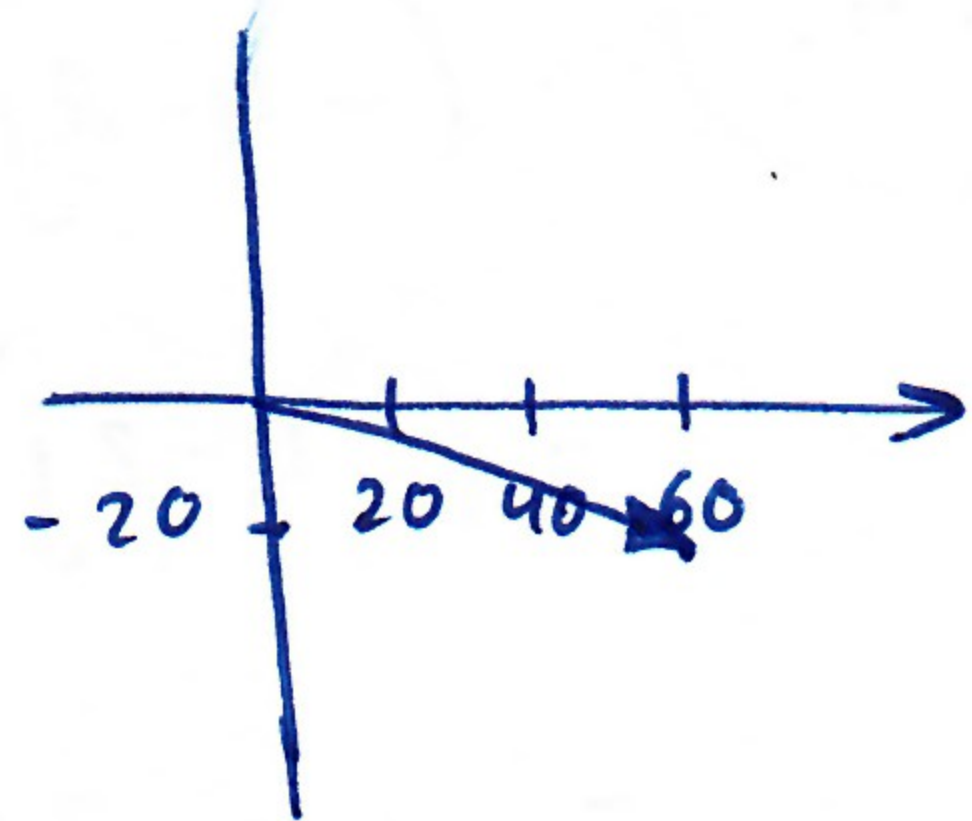


#28 $60 - 20j$ keep the radicals!

$$r = \sqrt{60^2 + (-20)^2} = \sqrt{3600 + 400} = \sqrt{4000} = 20\sqrt{10}$$

$$\theta_{\text{ref.}} = \tan^{-1} \frac{-20}{60} = \tan^{-1} -\frac{1}{3} \approx -18.4^\circ$$

$$\theta = -18.4^\circ \quad \text{or} \quad \theta = 360^\circ - 18.4^\circ = 341.6^\circ$$



$$60 - 20j = 20\sqrt{10} \angle -18.4^\circ = 20\sqrt{10} \angle 341.6^\circ$$

converting to radians: $\frac{\pi \cdot (-18.4^\circ)}{180^\circ} \approx -0.32$

$$\frac{\pi \cdot (341.6^\circ)}{180^\circ} \approx 5.96$$

$$60 - 20j = 20\sqrt{10} e^{-0.32j} = 20\sqrt{10} e^{5.96j}$$

#34. $48 (\cos 60^\circ + j \sin 60^\circ) = 48 \cdot 0.5 + 48 \cdot j \cdot \frac{\sqrt{3}}{2} \approx 24 + 41.6j$

#42 $e^{-3.62j} = 1 \angle -207.4^\circ = 1 (\cos(-207.4^\circ) + j \sin(-207.4^\circ))$

$$r = 1$$

$$\text{deg} = \frac{-3.62 \cdot 180^\circ}{\pi} \approx -207.4^\circ$$

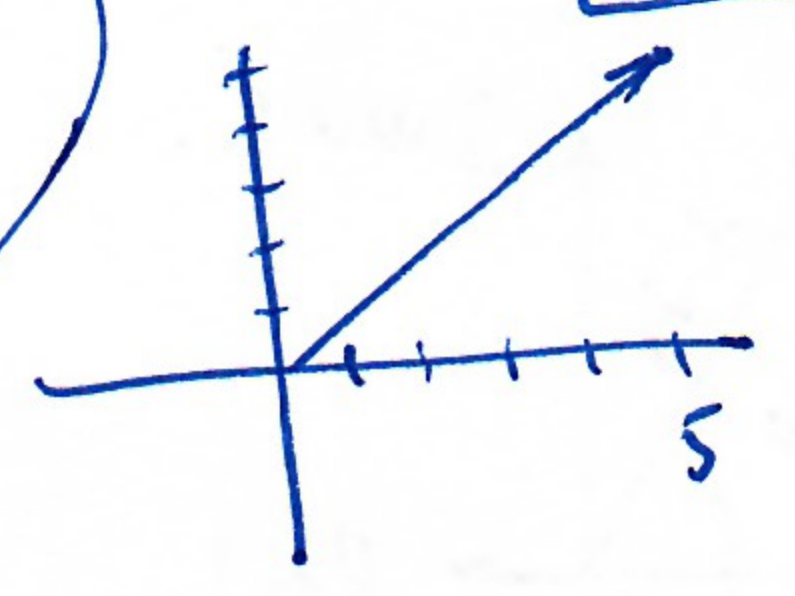
$$\approx -0.89 + 0.46j$$

#46 $2.5 \angle 162^\circ \cdot 8 \angle 115^\circ = \boxed{20 \angle 277^\circ}$

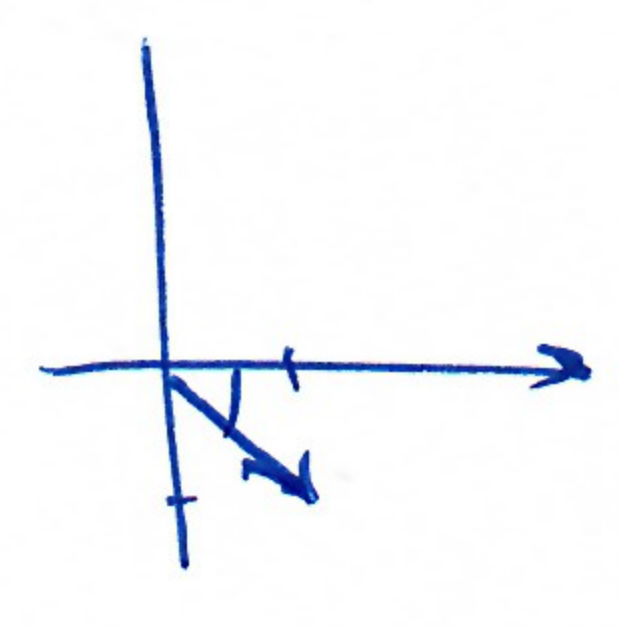
#57 $(2 \angle 16^\circ)^{10} = 2^{10} \angle 10 \cdot 16^\circ = \boxed{1024 \angle 160^\circ}$

#63 $\frac{(5+5j)^4}{(1-j)^6} = \frac{(5\sqrt{2} \angle 45^\circ)^4}{(\sqrt{2} \angle -45^\circ)^6} = \frac{5^4 \cdot 2^2 \angle 4 \cdot 45^\circ}{2^3 \angle 6 \cdot (-45^\circ)} = \frac{312.5 \angle 180^\circ}{8 \angle -270^\circ} = \frac{312.5 \angle 180^\circ}{8 \angle 90^\circ} = \boxed{312.5 \angle 90^\circ}$

$5+5j$ to polar form: $r = \sqrt{25+25} = \sqrt{50} = 5\sqrt{2}$
 $\theta_{ref.} = \tan^{-1} \frac{5}{5} = 45^\circ$

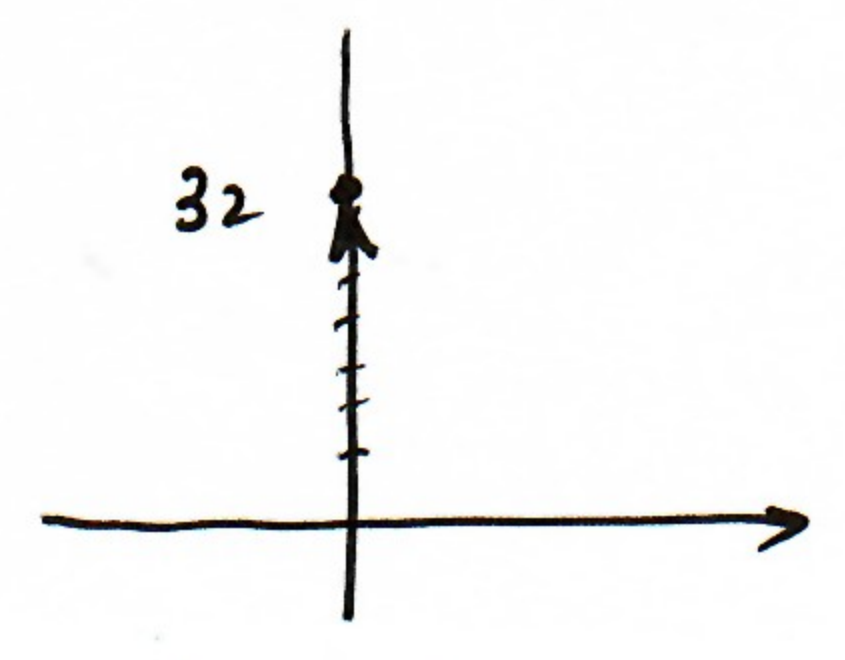


$1-j$ to polar form: $r = \sqrt{1+1} = \sqrt{2}$
 $\theta_{ref.} = \tan^{-1} \frac{-1}{1} = -45^\circ$
 $\theta = -45^\circ$ or 315°



#68 $x^5 - 32j = 0$
 $x^5 = 32j$
 $x = \sqrt[5]{32j}$
 $x = 2 \sqrt[5]{j}$

let's convert $32j$ to polar form:
 $r = \sqrt{0^2 + (32)^2} = \sqrt{32^2} = 32$
 $\tan^{-1} \frac{32}{0} \quad \theta = \frac{\pi}{2} = 90^\circ$

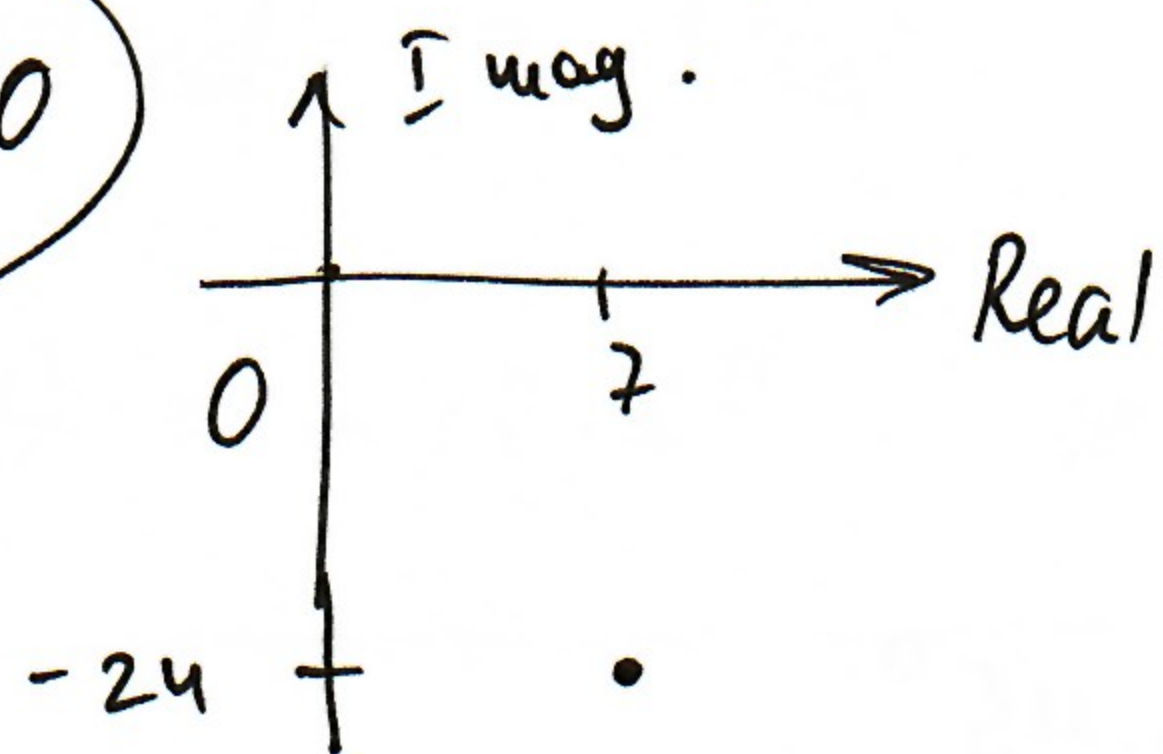


- 1st fifth root: $\sqrt[5]{32 \angle 45^\circ} = 2 \angle 9^\circ \approx 2 + 0.3j$
- 2nd fifth root: $\sqrt[5]{32 \angle 45^\circ + 360^\circ} = 2 \angle 81^\circ \approx 0.3 + 2j$
- 3rd fifth root: $\sqrt[5]{32 \angle 45^\circ + 720^\circ} = 2 \angle 153^\circ \approx -1.8 + 0.9j$

4th fifth root : $\sqrt[5]{32 \angle 45^\circ + 1080^\circ} = 2 \angle 225^\circ \approx -1.4 - 1.4j$

5th fifth root : $\sqrt[5]{32 \angle 45^\circ + 1440^\circ} = 2 \angle 297^\circ \approx 0.9 - 1.8j$

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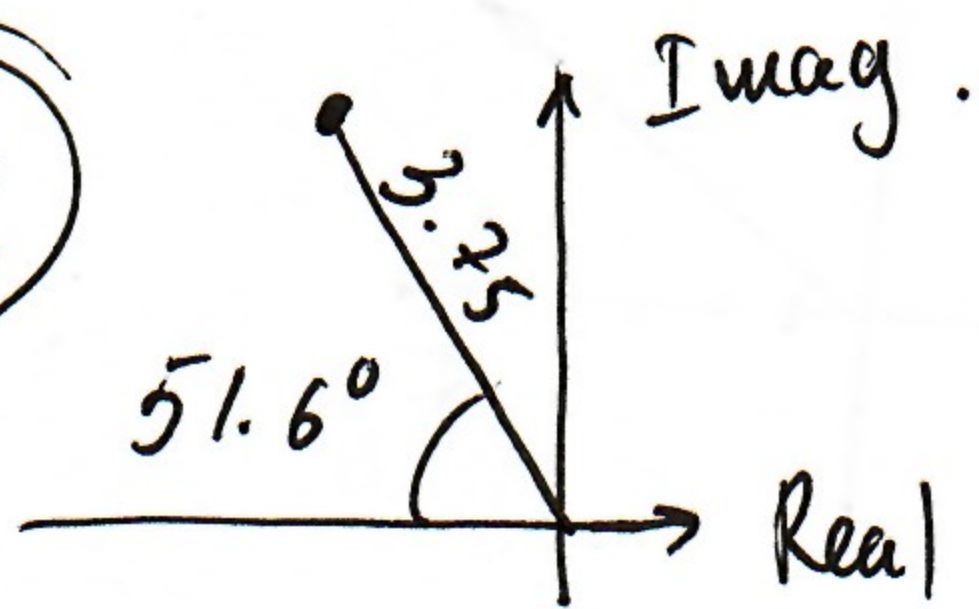


$7 - 24j = 25 \angle -74^\circ$

$\theta_{ref.} = \tan^{-1} \frac{-24}{7} \approx -74^\circ \quad \theta = -74^\circ$

$r = \sqrt{7^2 + (-24)^2} = \sqrt{625} = 25$

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$3.75 \angle 51.6^\circ$

$3.75 (\cos 51.6^\circ + j \sin 51.6^\circ) \approx 2.3 + 2.9j$