

1) Find the **running time $T(n)$** and the asymptotic running time (using Θ -notation and O -notation) of the following piece of code:

```
n = int(input("Enter an integer number greater than 2:"))

for i in range(n):      n iterations
    print(i)           1 step

for j in range(n):      n iterations
    print(j)           1 step
```

$$T(n) = n+n = 2n$$

$$T(n) = \Theta(n)$$

2) Find the **running time $T(n)$** and the asymptotic running time (using Θ -notation and O -notation) of the following piece of code:

```
n = int(input("Enter an integer number greater than 10:"))

for i in range(n):      n iterations
    for j in range(n):  n iterations
        print(i, "\t", j) 1 step
```

$$T(n) = n*n*1 = n^2$$

$$T(n) = \Theta(n^2)$$

3) Find the **running time $T(n)$** and the asymptotic running time (using Θ -notation and O -notation) of the following piece of code:

```
n = int(input("Enter an integer number greater than 12:"))

while n>1:
    print(n)           1 step
    n = n//2          each time n becomes "twice less", until eventually it is <= 1, 2 steps

print(n)              1 step
```

$$T(n) = 3\log_2 n + 1$$

$$T(n) = \Theta(\log n)$$

1) Copy the following program (you may omit the docstring):

```
def summation1(n):
    """ finds the sum (n+i)^2/i, where i runs from 1 to n

    pre: n in positive integer
    post: returns a positive integer number."""
    sum = 0
    for elem in list(range(n)):
        sum += (n+1+elem)**2/(elem+1)
    return sum
```

$$\sum_{i=1}^n \frac{(n+i)^2}{i}$$

2) run the defined procedure on different inputs, for example $n = 1, 2, 10$.
Write down the results.

```
4.0
17.0
547.8968253968254
```

3) Write, following the code of the program, each call of this procedure on inputs $n = 1, 2, 10$ as a sum of fractions, i.e. write which sum finds for procedure for each of these calls, but don't calculate it.

n=1 list: 0	n=2 list = 0,1	n=10 list = 0,1,2,3,4,5,6,7,8,9
sum: $0 + \frac{2^2}{1}$	sum: $0 + \frac{3^2}{1} + \frac{4^2}{2}$	sum: $0 + \frac{11^2}{1} + \frac{12^2}{2} + \frac{13^2}{3} + \frac{14^2}{4} + \frac{15^2}{5} + \frac{16^2}{6} + \frac{17^2}{7} + \frac{18^2}{8} + \frac{19^2}{9} + \frac{20^2}{10}$
as expected	as expected	as expected

4) find the running time of the procedure (depending on n), assuming that it takes one unit of time for each of math operations; the assignment operator and `range` function take also one time unit, and function `list` takes n time units.

```
sum = 0                                1 step/ time unit
for elem in list(range(n)):             range(n): 1 step;    list: n steps
n iterations
    sum += (n+1+elem)**2/(elem+1)
    ↑↑↑↑↑                               7 steps → 7n steps
    ↑↑↑↑↑                               (we have n
return sum                               1 step          iterations,
                                                                with 7 steps each)
```

Therefore, $T(n) = 1+1+n+7n+1 = 3+8n$

5) What is the order of growth (in terms of O and Θ)?

$O(n), \Theta(n)$